

**Written Homework #6**  
**ChE 231**  
**Spring 2019**

Problem 1. Consider the matrix:

$$\mathbf{A} = \begin{bmatrix} 1 & 1 & 0 \\ 0 & 2 & 0 \\ 0 & -1 & 4 \end{bmatrix}$$

1. Calculate the eigenvalues.
2. Calculate the eigenvectors.
3. Use the modal matrix  $\mathbf{X}$  to diagonalize the matrix  $\mathbf{A}$ .

Problem 2. Consider an isothermal, continuous stirred tank reactor in which the following irreversible reaction occurs:  $A \rightarrow B$ . Let  $C_A$  and  $C_B$  denote the molar concentrations of the reaction species. The reaction rate constant is denoted  $k$ , and the reaction rate per unit volume is:  $r = kC_A$ . Let  $V$  denote the constant reactor volume, and  $q$  denote the volumetric flow rate of the inlet and outlet streams. The reactor is fed with pure component  $A$  at a molar concentration  $C_{Af}$ . Consider the following constant operating conditions:  $C_{Af} = 1$ , and  $V = 1$ . To determine the unknown reaction rate constant  $k$ , steady-state experiments were performed at three different volumetric flow rates. The following data  $\{\bar{q}, \bar{C}_A\}$  was obtained:  $\{0.5, 0.35\}$ ,  $\{1.0, 0.45\}$ ,  $\{2.0, 0.70\}$ . Steady-state component balances combined with the experimental data yield the following overdetermined set of linear algebraic equations:

$$\begin{bmatrix} 0.350 \\ 0.450 \\ 0.700 \end{bmatrix} k = \begin{bmatrix} 0.325 \\ 0.550 \\ 0.600 \end{bmatrix}$$

1. Formulate and analytically solve the least-square parameter estimation problem to obtain an estimate of  $k$ .
2. Compare the least-squares estimate of  $k$  to the estimates obtained from each individual experiment and the estimate obtained as the average of the individual estimates.